

 **Сюжеты, возникающие при обучении больших нейросетевых моделей.**

Даня Меркулов

```
RuntimeError: cuda runtime error (2) : out of memory at /data/users/soumith/miniconda2/cond
```

how can i solve this error?



apaszke commented on Mar 8, 2017

Member



You're running out of memory on the GPU. It's not a bug.



16



3

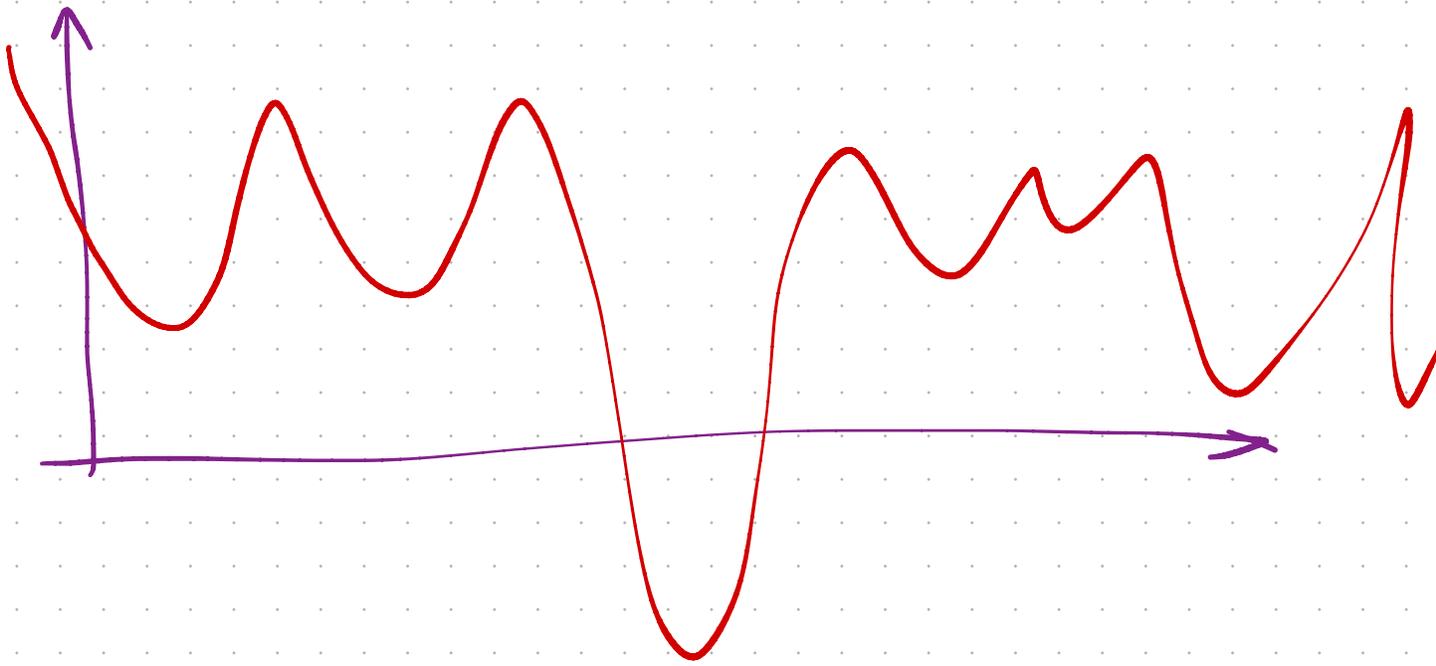
$P \approx 160 \cdot 10^9$   $\min_{x \in \mathbb{R}^P}$   $\frac{1}{N} \sum_{i=1}^N f_i(x) = f(x)$   $N \approx 10^{10}, 10^{11}$   
одна выборка

$$\nabla f = \frac{1}{N} \sum_{i=1}^N \nabla f_i(x)$$



# Large batch training

$g \approx \nabla f$   $g = \frac{1}{b} \sum_{i=1}^b \nabla f_i(x)$   $b = 64$   
 $128$   
 $256$



БОЛГ WE  $\rightarrow$  мейнш  
 гуенеренш  
 ПАРА ЛАФА ИЗМ.  $g$

MEGATRON  
DEEP SPEED

$X_k$

$g_k$

$$X_{k+1} = X_k - \eta \cdot g_k$$

$$X_{k+t} = X_k - \sum_{i=k}^{k+t} \eta \cdot g_i$$

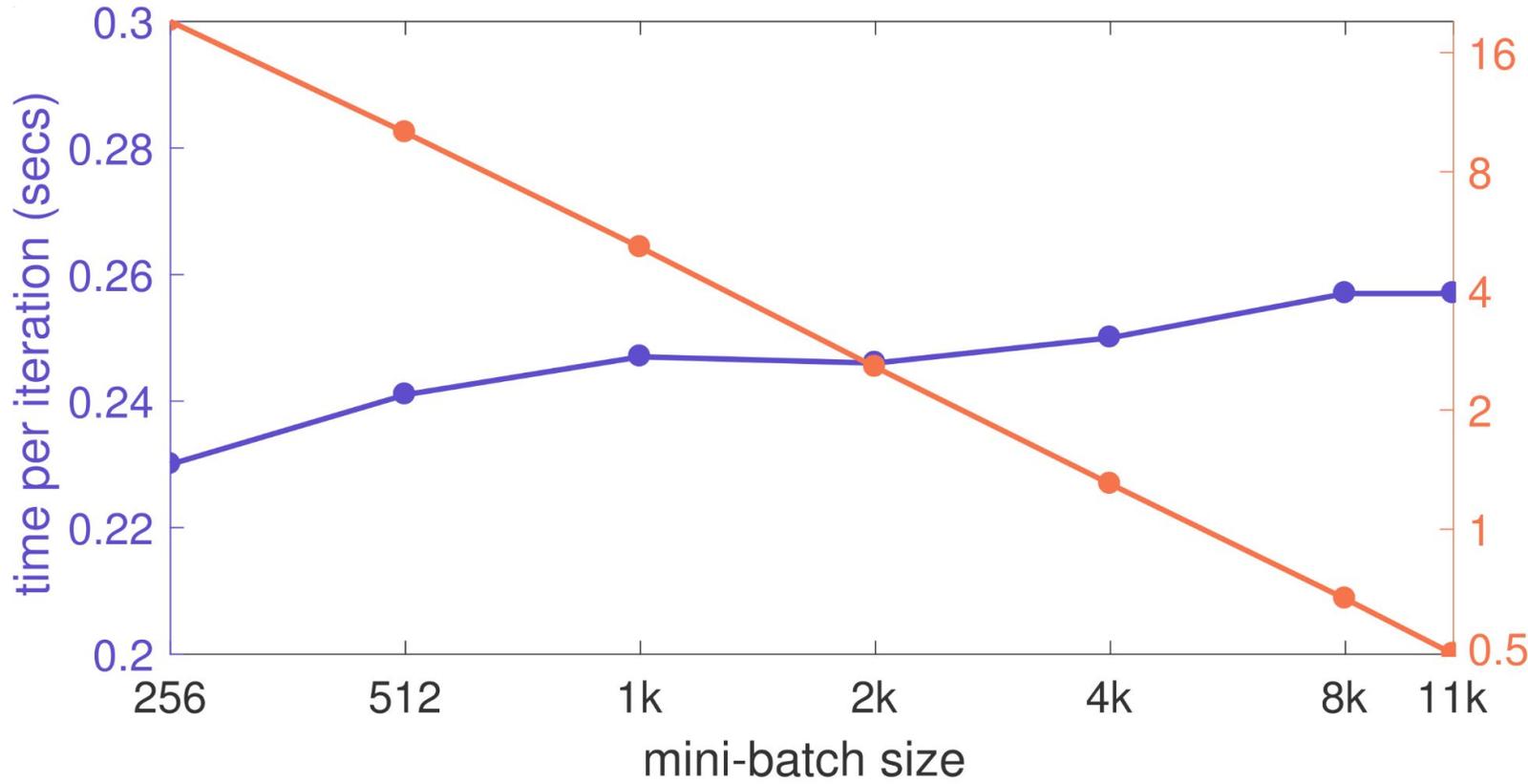
$$X_{k+1} = X_k - t \cdot \eta \cdot g_k$$

# Размер батча и время, затрачиваемое на одну эпоху.

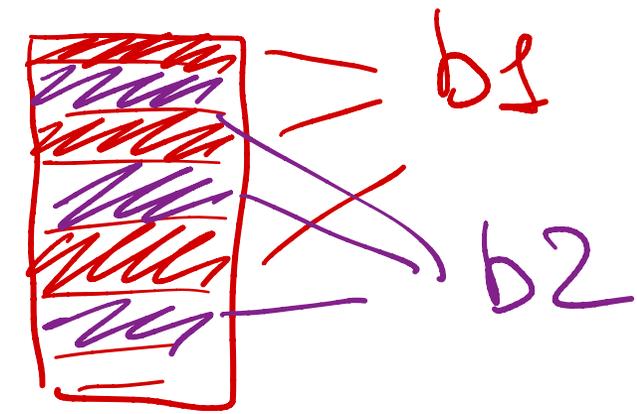
$b = 10^2$   
 $10^8$  шагов  $10^{10}$

$b = 10^5$  iter per epoch

$10^5$



При наличии достаточной памяти GPU, увеличение размера батча позволяет утилизировать ресурсы параллельных вычислений.



**Paper**  
 Accurate, Large Minibatch SGD: Training ImageNet in 1 Hour.

# Просто так увеличить размер батча не получится.

| $kn$ | $\eta$                   | top-1 error (%)  |
|------|--------------------------|------------------|
| 256  | 0.05                     | 23.92 $\pm$ 0.10 |
| 256  | 0.10                     | 23.60 $\pm$ 0.12 |
| 256  | 0.20                     | 23.68 $\pm$ 0.09 |
| 8k   | 0.05 $\cdot$ 32          | 24.27 $\pm$ 0.08 |
| 8k   | 0.10 $\cdot$ 32          | 23.74 $\pm$ 0.09 |
| 8k   | 0.20 $\cdot$ 32          | 24.05 $\pm$ 0.18 |
| 8k   | 0.10                     | 41.67 $\pm$ 0.10 |
| 8k   | 0.10 $\cdot$ $\sqrt{32}$ | 26.22 $\pm$ 0.03 |

Обучение ResNet-50 на датасете ImageNet с разными вариантами увеличения размера батча.

(a) **Comparison of learning rate scaling rules.** A reference learning rate of  $\eta = 0.1$  works best for  $kn = 256$  (23.68% error). The linear scaling rule suggests  $\eta = 0.1 \cdot 32$  when  $kn = 8k$ , which again gives best performance (23.74% error). Other ways of scaling  $\eta$  give worse results.



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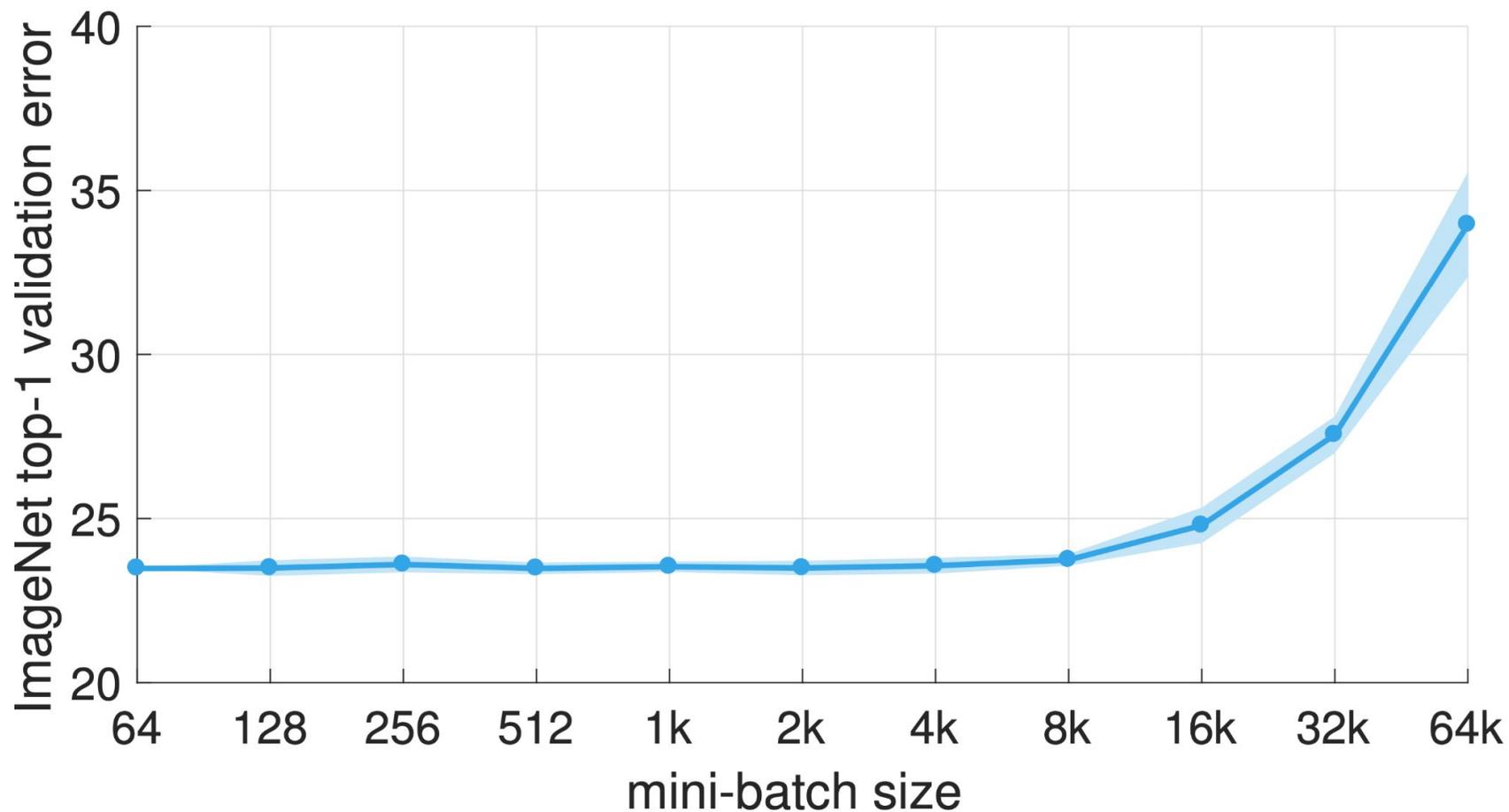
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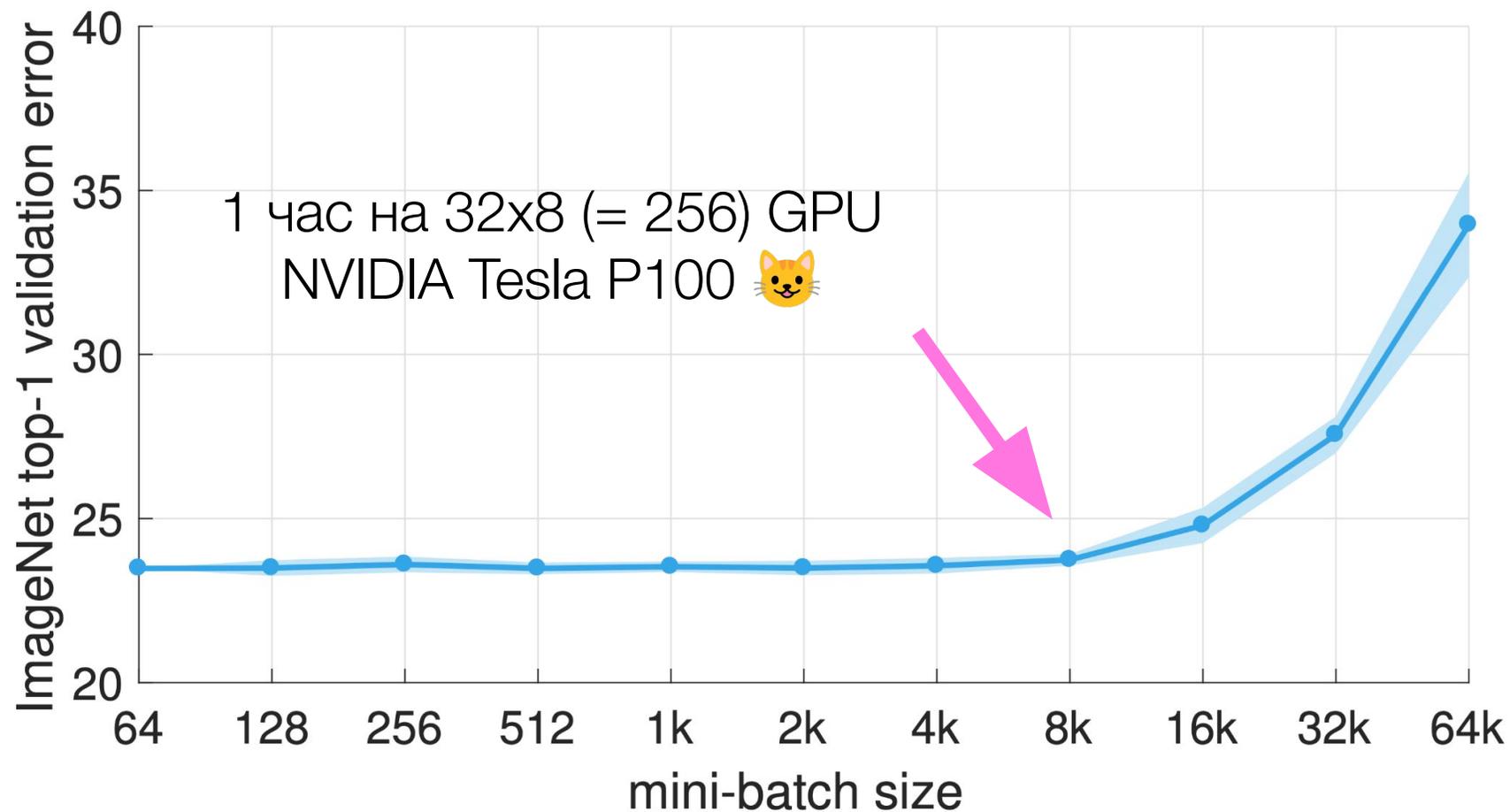
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# Как увеличивать размер батча?

## 1. Linear scaling rule.

При увеличении размера батча в  $k$  раз, learning rate увеличивать тоже в  $k$  раз:

$$\hat{\alpha} = k\alpha$$

$$\hat{\alpha} = \sqrt{k} \cdot \alpha$$

## 2. Gradual warmup.

На первых эпохах (итерациях) learning rate увеличивать постепенно от начального до целевого.

## 3. Square root scaling rule



**Paper**

Accurate, Large Minibatch SGD: Training ImageNet in 1 Hour.



**Paper**

Learning Rates as a Function of Batch Size: A Random Matrix Theory Approach to Neural Network Training.

# Как ещё увеличивать размер батча?

LARS (Layer-wise Adaptive Rate Scaling):

Linear scaling rule + для каждого слоя свой learning rate, который шкалируется на норму весов этого слоя.

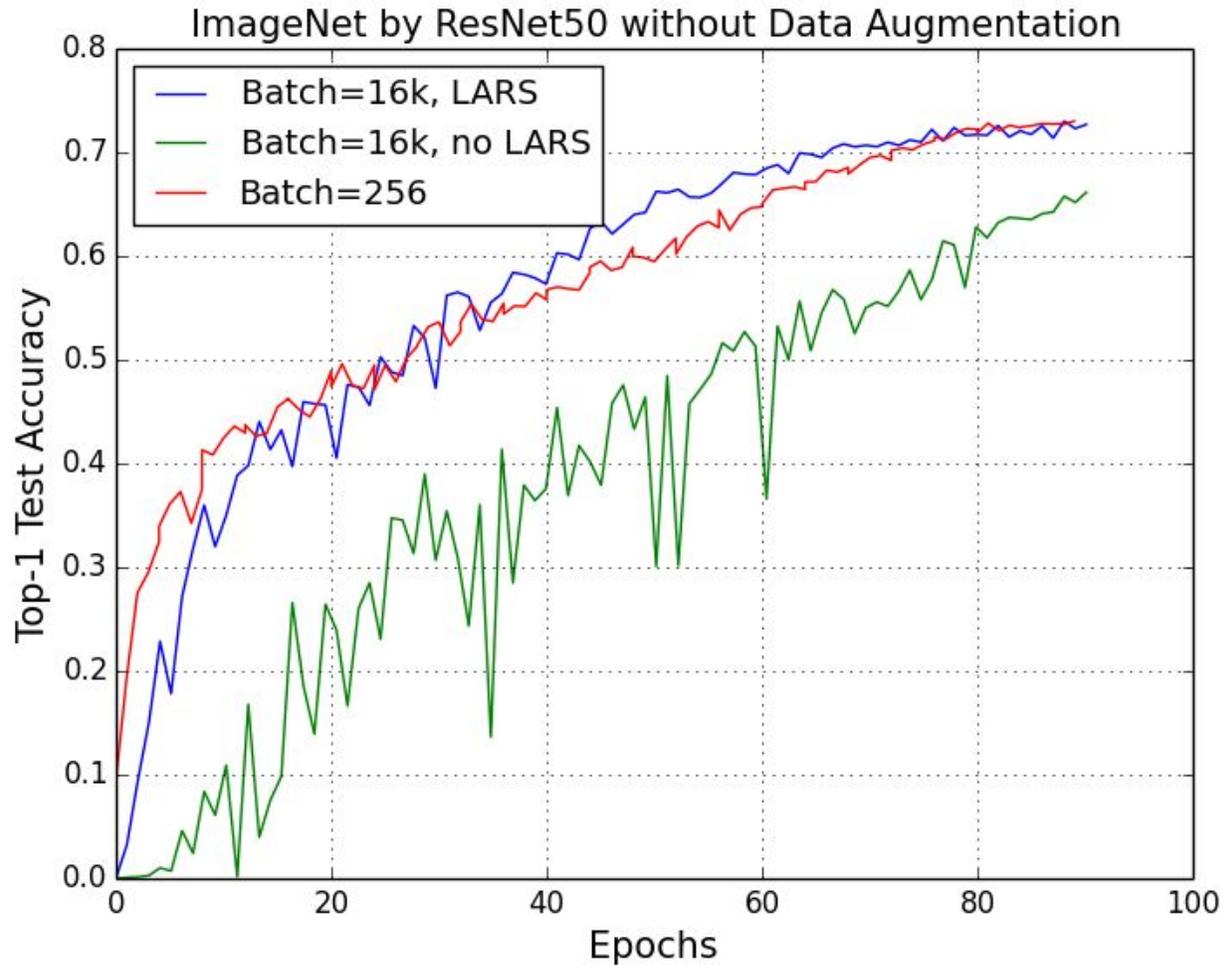
$$\hat{\alpha}_l = k\alpha_l \frac{\|w_l\|_2}{\|\nabla_{w_l} L\|_2},$$
$$l = 1, \dots, N_{layers}$$



**Paper**

Large batch training of convolutional networks.

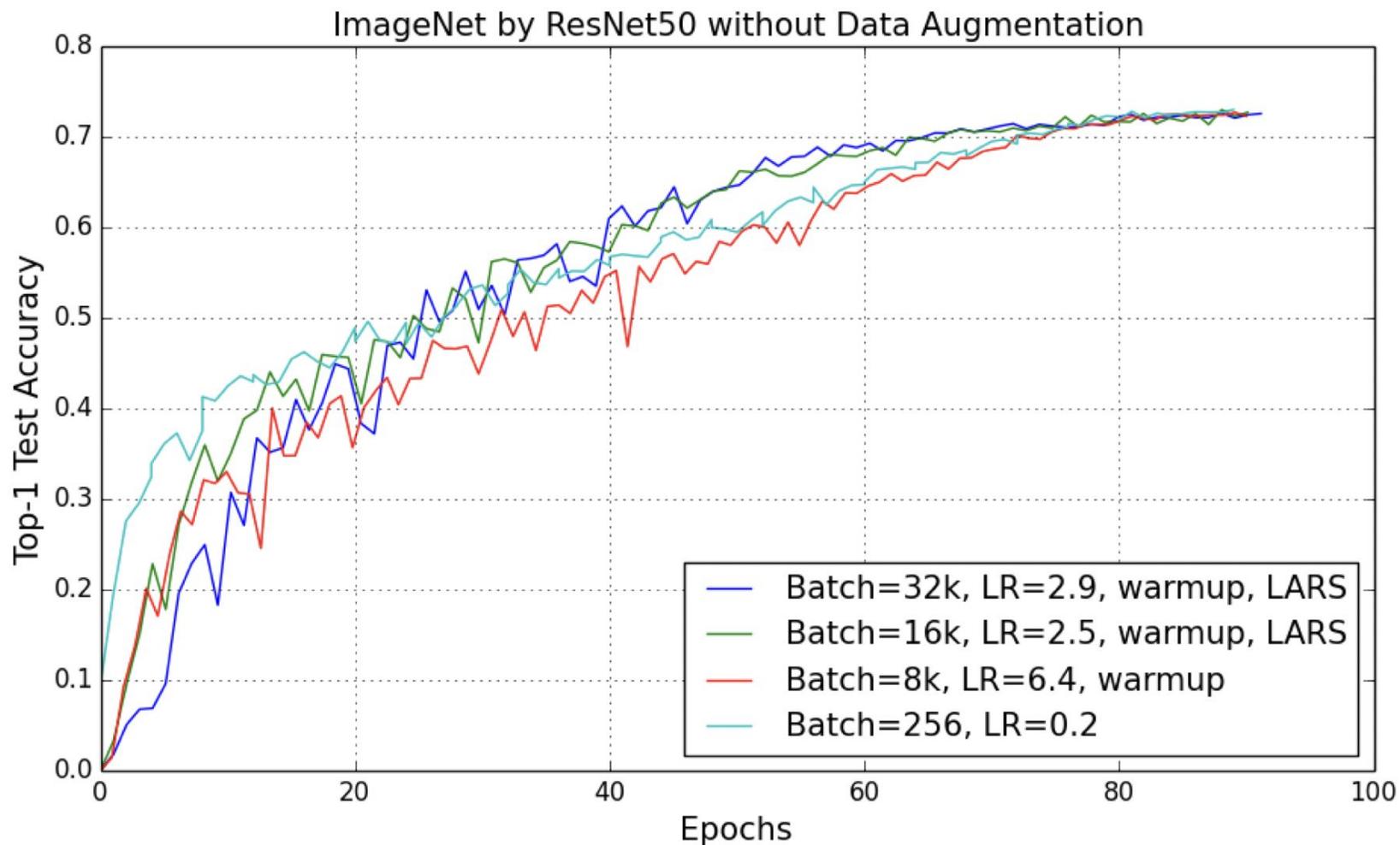
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# Как ещё увеличивать размер батча?

LAMB = LARS + Adam 🦄

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## Algorithm 1 LARS

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**Input:**  $x_1 \in \mathbb{R}^d$ , learning rate  $\{\eta_t\}_{t=1}^T$ , parameter  $0 < \beta_1 < 1$ , scaling function  $\phi$ ,  $\epsilon > 0$

Set  $m_0 = 0$

**for**  $t = 1$  to  $T$  **do**

Draw  $b$  samples  $S_t$  from  $\mathbb{P}$

Compute  $g_t = \frac{1}{|S_t|} \sum_{s_t \in S_t} \nabla \ell(x_t, s_t)$

$m_t = \beta_1 m_{t-1} + (1 - \beta_1)(g_t + \lambda x_t)$

$x_{t+1}^{(i)} = x_t^{(i)} - \eta_t \frac{\phi(\|x_t^{(i)}\|)}{\|m_t^{(i)}\|} m_t^{(i)}$  for all  $i \in [h]$

**end for**

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**Paper**

Large batch optimization for Deep  
Learning: training BERT in 76 minutes.

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## Algorithm 2 LAMB

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**Input:**  $x_1 \in \mathbb{R}^d$ , learning rate  $\{\eta_t\}_{t=1}^T$ , parameters  $0 < \beta_1, \beta_2 < 1$ , scaling function  $\phi$ ,  $\epsilon > 0$

Set  $m_0 = 0, v_0 = 0$

**for**  $t = 1$  to  $T$  **do**

Draw  $b$  samples  $S_t$  from  $\mathbb{P}$ .

Compute  $g_t = \frac{1}{|S_t|} \sum_{s_t \in S_t} \nabla \ell(x_t, s_t)$ .

$m_t = \beta_1 m_{t-1} + (1 - \beta_1) g_t$

$v_t = \beta_2 v_{t-1} + (1 - \beta_2) g_t^2$

$m_t = m_t / (1 - \beta_1^t)$

$v_t = v_t / (1 - \beta_2^t)$

Compute ratio  $r_t = \frac{m_t}{\sqrt{v_t + \epsilon}}$

$x_{t+1}^{(i)} = x_t^{(i)} - \eta_t \frac{\phi(\|x_t^{(i)}\|)}{\|r_t^{(i)} + \lambda x_t^{(i)}\|} (r_t^{(i)} + \lambda x_t^{(i)})$

**end for**

---

## Как ещё увеличивать размер батча? LAMB.

| Solver   | batch size | steps | F1 score on dev set | TPUs | Time   |
|----------|------------|-------|---------------------|------|--------|
| Baseline | 512        | 1000k | 90.395              | 16   | 81.4h  |
| LAMB     | 512        | 1000k | 91.752              | 16   | 82.8h  |
| LAMB     | 1k         | 500k  | 91.761              | 32   | 43.2h  |
| LAMB     | 2k         | 250k  | 91.946              | 64   | 21.4h  |
| LAMB     | 4k         | 125k  | 91.137              | 128  | 693.6m |
| LAMB     | 8k         | 62500 | 91.263              | 256  | 390.5m |
| LAMB     | 16k        | 31250 | 91.345              | 512  | 200.0m |
| LAMB     | 32k        | 15625 | 91.475              | 1024 | 101.2m |
| LAMB     | 64k/32k    | 8599  | 90.584              | 1024 | 76.19m |



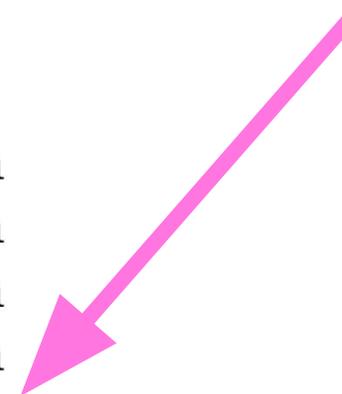
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76 минут  
на 1024 TPU 🐱



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# Gradient accumulation

Идея аккумуляции градиента.

$$g = \frac{1}{b} \sum_{i=1}^b \nabla f_i(x)$$

$$\tilde{b} = 1 \text{ (влезно)}$$

$$g_1 = \nabla f_{i_1}(x)$$

$$g_2 = \frac{\nabla f_{i_2}(x)}{10}$$

$$\vdots$$
$$g_{10} = \frac{\nabla f_{i_{10}}(x)}{10}$$

$$g_1 + \dots + g_{10} = \hat{g}$$

$$x_{k+1} = x_k - \hat{g}$$

# Gradient accumulation

 БЫЛО:

```
# loop through batches
for (inputs, labels) in data_loader:

    # extract inputs and labels
    inputs = inputs.to(device)
    labels = labels.to(device)

    # passes and weights update
    with torch.set_grad_enabled(True):

        # forward pass
        preds = model(inputs)
        loss = criterion(preds, labels)

        # backward pass
        loss.backward()

        # weights update
        optimizer.step()
        optimizer.zero_grad()
```

 СТАЛО:

```
# batch accumulation parameter
accum_iter = 4

# loop through enumerate batches
for batch_idx, (inputs, labels) in enumerate(data_loader):

    # extract inputs and labels
    inputs = inputs.to(device)
    labels = labels.to(device)

    # passes and weights update
    with torch.set_grad_enabled(True):

        # forward pass
        preds = model(inputs)
        loss = criterion(preds, labels)

        # normalize loss to account for batch accumulation
        loss = loss / accum_iter

        # backward pass
        loss.backward()

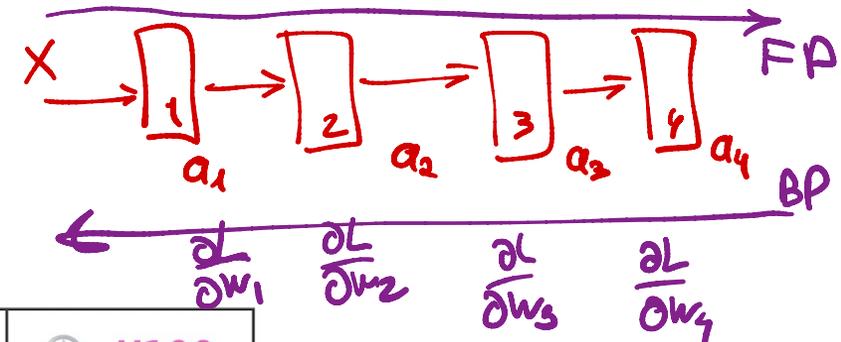
        # weights update
        if ((batch_idx + 1) % accum_iter == 0) or (batch_idx + 1 == len(data_loader)):
            optimizer.step()
            optimizer.zero_grad()
```



# Ссылки



# Ссылки. Gradient checkpointing.



Checkpointing

**Site**  
Training larger-than-memory PyTorch models using gradient checkpointing.

|   | Batch Size | Memory  | T4        | V100    |
|---|------------|---------|-----------|---------|
| ✗ | 64         | 9.42 GB | 47m 30s   | 18m 51s |
| ✓ | 64         | 3.71 GB | 1h 0m 34s | 23m 48s |

**Site**  
Hugging Face. Efficient training on a single GPU.

```
training_args = TrainingArguments(
    per_device_train_batch_size=1, gradient_accumulation_steps=4, gradient_checkpointing=True,
)
```

GPT3small\_Puskin without checkpointing (batch = 8, sec\_len = 512)

| index      | used_mem | delta_mem | delta_time | + | ... |
|------------|----------|-----------|------------|---|-----|
| begin      | 5804     | 0         | 0          |   |     |
| forward    | 13006    | 7202      | 0.04       |   |     |
| backward   | 14576    | 8772      | 1.2        |   |     |
| optim_step | 14576    | 8772      | 0.02       |   |     |
| end        | 5840     | 36        | 0.13       |   |     |
| total      | 15109.75 | 0         | 1.396      |   |     |

GPT3small\_Puskin with checkpointing (batch = 8, sec\_len = 512)

| index      | used_mem | delta_mem | delta_time | + | ... |
|------------|----------|-----------|------------|---|-----|
| begin      | 4828     | 0         | 0          |   |     |
| forward    | 6398     | 1570      | 0.45       |   |     |
| backward   | 7968     | 3140      | 1.14       |   |     |
| optim_step | 7968     | 3140      | 0.05       |   |     |
| end        | 4828     | 0         | 0.01       |   |     |
| total      | 15109.75 | 0         | 1.655      |   |     |



# Ссылки. Activation quantization.



## Repository

FewBit - Compression schema for gradient of activations in backward pass

|   | Task | Batch Size | GELU    | Linear Layer | Peak Memory, GiB | Saving, % |
|---|------|------------|---------|--------------|------------------|-----------|
| 1 | MRPC | 128        | Vanilla | Vanilla      | 11.30            | 0.0       |
| 2 | MRPC | 128        | 3-bit   | Vanilla      | 9.75             | 13.8      |
| 3 | MRPC | 128        | Vanilla | Randomized   | 9.20             | 18.6      |
| 4 | MRPC | 128        | 3-bit   | Randomized   | 7.60             | 32.7      |

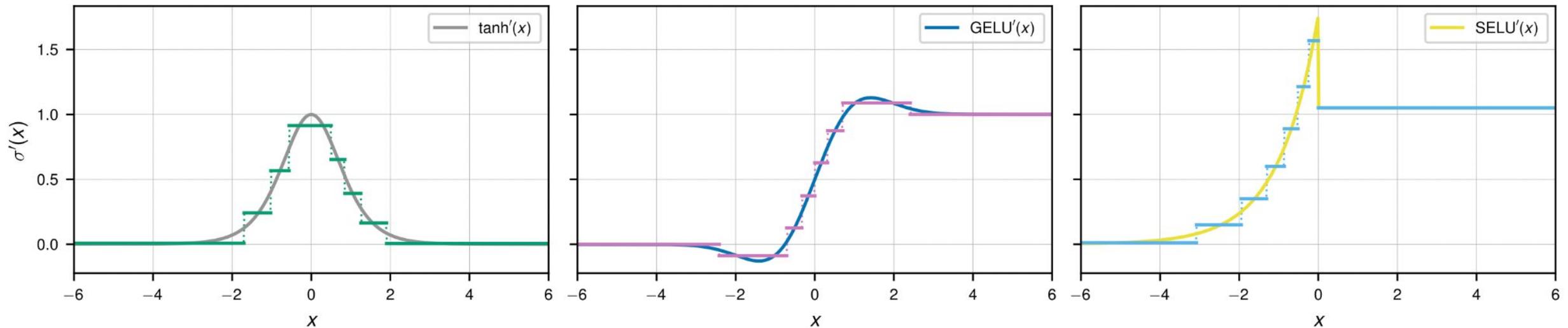


Figure 1. Optimized 3-bit piecewise-constant approximations of the derivatives of activation functions.



# Ссылки. Automatic Mixed Precision training.



## Repository

Automatic Mixed Precision Tutorials using pytorch

Fine-tuning **32-bit** model for 215 iterations.

Time: **01:32**

Peak GPU memory consumption: **8325 MB**

Loss: 2.7370730377906978

Fine-tuning **16-bit** model for 215 iterations.

Time: 01:01

Peak GPU memory consumption: **6691 MB**

Loss: 2.737271473019622

*Gradient descent without gradient  
Learning to learn*



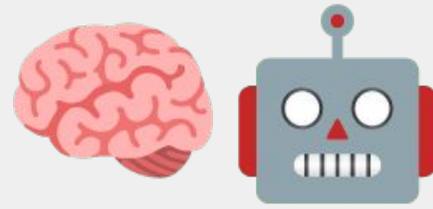
## Site

PyTorch: CUDA Automatic Mixed Precision training examples

- B : Baseline (FP32)
- AMP : Automatic Mixed Precision Training (AMP)

| Algorithm     | Test Accuracy | GPU Memory | Total Training Time |
|---------------|---------------|------------|---------------------|
| B - 1080 Ti   | 94.13         | 10737MB    | 64.9m               |
| B - 2080 Ti   | 94.17         | 10855MB    | 54.3m               |
| AMP - 1080 Ti | 94.07         | 6615MB     | 64.7m               |
| AMP - 2080 Ti | 94.23         | 7799MB     | 37.3m               |

Post-local SGD



# Практика